Let $M$ be the moduli space of semistable rank 2 Higgs pairs $(V, \phi)$ with trivial determinant over a smooth projective curve $X$ of genus $g \geq 2$. We compute the stringy E-function of $M$ and prove that there does not exist a symplectic desingularization of $M$ for $g \geq 3$.